## 5.111 Lecture Summary #13

**Readings for today:** Section 3.8 – 3.11 Molecular Orbital Theory (Same in 5<sup>th</sup> and 4<sup>th</sup> ed.) **Read for Lecture #14:** Sections 3.4, 3.5, 3.6 and 3.7 – Valence Bond Theory (Same in 5<sup>th</sup> and 4<sup>th</sup> ed).

## Topics: I. Molecular orbital theory

- **A.** Homonuclear molecules with MOs originating from s orbitals
- **B.** Homonuclear molecules with MOs originating from s and p orbitals
- C. Heteronuclear diatomic molecules

#### I. MOLECULAR ORBITAL (MO) THEORY

In MO theory, valence electrons are \_\_\_\_\_\_ over the entire molecule, not confined to individual atoms or bonds, as in Lewis and valence-bond models.

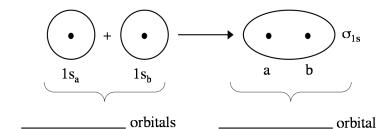
Molecular orbitals (\_\_\_\_\_\_\_) of diatomic molecules arise from adding together (superimposing) atomic orbitals.

A Linear Combination of Atomic Orbitals (LCAO) creates molecular orbitals (bonding orbitals and antibonding orbitals)

*N* molecular orbitals can be constructed by *N* atomic orbitals.

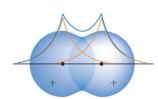
# A. Homonuclear molecules with MOs originating from s orbitals

Bonding orbitals arise from LCAO under conditions of constructive interference



σ: designates a molecular orbital that is cylindrically symmetric about the bond axis (with no nodal plane along the bond axis).

 $\underline{\hspace{1cm}}$  +  $\underline{\hspace{1cm}}$  =  $\sigma_{1s}$  = bonding molecular orbital (MO) and also a **wavefunction**.



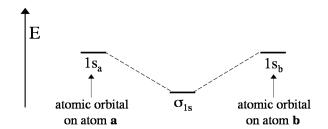
When waves interfere <u>constructively</u>, the amplitude **increases** where they overlap.

**Increased** amplitude in the internuclear region translates to an **enhanced** probability density  $(\psi^2)$  between the nuclei.

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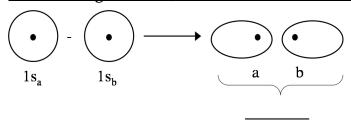
Any electron that occupies a bonding MO will be attracted to BOTH nuclei, and therefore will be \_\_\_\_\_\_ compared to an atomic orbital associated with a single nucleus.

**Energy of interaction**. The energy of a **bonding orbital** is \_\_\_\_\_ compared to the atomic orbitals!

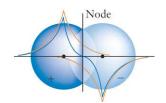


For H<sub>2</sub>, when its two electrons both occupy the bonding orbital, the molecule is \_\_\_\_\_stable.

#### **Antibonding orbitals** (result of **destructive** interference of two atomic orbitals)



 $\underline{\phantom{a}}$  -  $\underline{\phantom{a}}$  =  $\sigma_{1s}^*$  = antibonding molecular orbital.



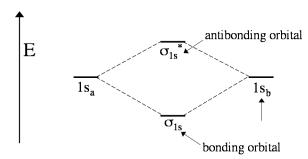
When wavefunctions interfere **destructively**, the amplitude **decreases** where they overlap.

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**Decreased** amplitude in the internuclear region translates to a **diminished** probability density  $(\psi^2)$  between the nuclei and a **node** between the two nuclei.

An electron in this **antibonding orbital** would be essentially excluded from the internuclear region, and thus have a \_\_\_\_\_\_ energy than if in an atomic orbital.

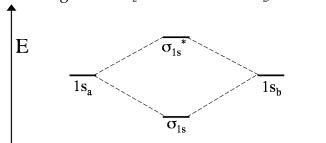
**Energy of interaction**. The energy of an **antibonding orbital** is\_\_\_\_\_\_ compared to the atomic orbitals!



An antibonding orbital is raised in energy by approximately the same amount that the bonding orbital is lowered in energy.

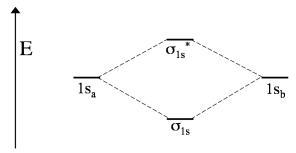
N molecular orbitals can be constructed by N atomic orbitals. Thus, 2 atomic orbitals generate 2 molecular orbitals (one bonding and one antibonding, one lower in energy and one higher in energy).

MO diagram of  $H_2$ : In the case of  $H_2$ , both electrons are in the  $\sigma_{1s}$  orbital.



Electron configuration of H<sub>2</sub>: \_\_\_\_\_

MO diagram of He<sub>2</sub>:



Electron configuration of He<sub>2</sub>: \_\_\_\_\_interest is \_\_\_\_\_interest in the energy for He<sub>2</sub> compared to 2 He.

MO theory predicts He<sub>2</sub> does not exist because no net gain in E.

BOND ORDER =  $\frac{1}{2}$  (# of bonding electrons - # of antibonding electrons)

He<sub>2</sub>:  $(\sigma_{1s})^2(\sigma_{1s}^*)^2$ 

bond order = bond

 $H_2: (\sigma_{1s})^2$ 

bond order = \_\_\_\_\_ bond

Reality: He<sub>2</sub> does exist. 'Discovered' in 1993. Weakest chemical bond known.

 $\Delta E_d = 0.01 \text{ kJ/mol for He}_2$  $\Delta E_d = 432 \text{ kJ/mol for H}_2$ 

The MOs formed by LCAO for 2s orbitals are analogous to those formed by 1s.

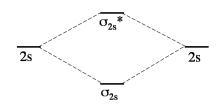
 $Li_2$ 

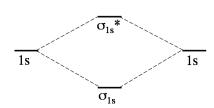
Electron configuration:  $(\sigma_{1s})^2(\sigma_{1s}^*)^2(\sigma_{2s})^2$ 

Bond order:  $\frac{1}{2}$  ( ) =

 $\Delta E_d =$ \_\_\_\_\_kJ/mol

**1** 





Note: Bond order can be calculated by considering all electrons or only valence electrons.

 $Be_2$ 

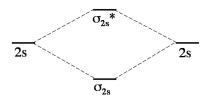
 $e^{-}$  configuration:  $(\sigma_{1s})^2(\sigma_{1s}^*)^2(\sigma_{2s})^2(\sigma_{2s}^*)^2$ 

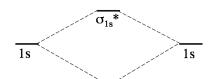
Bond order (counting all electrons): ½ ( ) =

Bond order (counting only valence e<sup>-</sup>s): ½ ( ) =

 $\Delta E_d = \underline{\hspace{1cm}} kJ/mol - very weak$ 

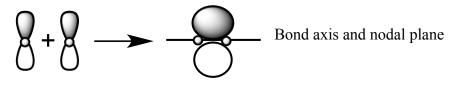
E





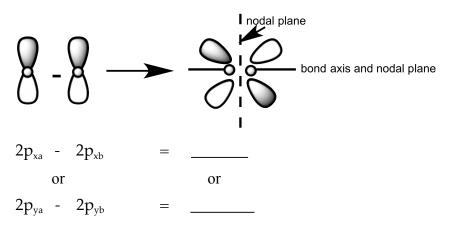
# B. Homonuclear molecules with MOs originating from s and p orbitals

**Bonding MO**s formed by LCAO of  $2p_x$  and  $2p_y$  as a result of **constructive** interference



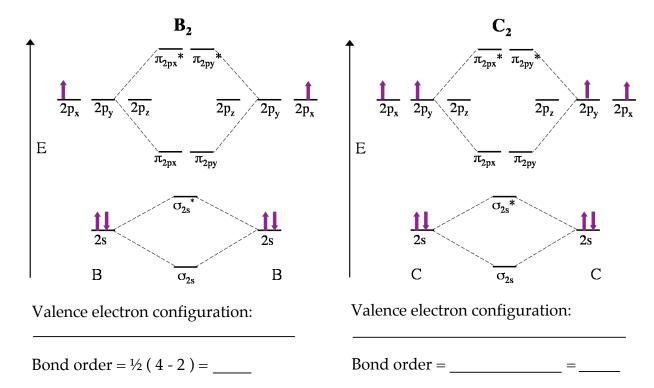
 $\pi$ -orbital: Molecular wavefunction (molecular orbital) with a nodal plane through the \_\_\_\_\_ axis.

Antibonding MOs formed by LCAO of 2p<sub>x</sub> and 2p<sub>y</sub> as a result of destructive interference



 $\pi^*$ -orbitals: Molecular wavefunction (molecular orbital) with TWO nodal planes. One nodal plane is through the bonding axis and the other is between nuclei.

Please note that MO diagrams for  $B_2$  and  $C_2$  below are incomplete since they do not include the  $2p_z$  molecular orbitals!



Just considering 2s, 2p<sub>x</sub>, and 2p<sub>y</sub> for the moment, let's sum it up:

**Two** 2s AOs generate **two**  $\sigma_{2s}$  MOs (lower energy  $\sigma_{2s}$  & higher energy  $\sigma_{2s}$ \*).

**Two**  $2p_x$  AOs generate **two**  $\pi_{2px}$  MOs (lower energy  $\pi_{2px}$  & higher energy  $\pi_{2px}^*$ ). **Two**  $2p_y$  AOs generate **two**  $\pi_{2py}$  MOs (lower energy  $\pi_{2py}$  & higher energy  $\pi_{2py}^*$ )

The stability of the resulting molecule depends on the # electrons that occupy lower energy orbitals compared to the # that occupy higher energy orbitals.

If the net result of molecule formation is that more electrons have a lower energy, then the molecule is \_\_\_\_\_.

If the energy differential is small, then the molecule is not as stable.

For B<sub>2</sub>: 
$$(\sigma_{2s})^2(\sigma_{2s}^*)^2\pi_{2px}\pi_{2py}^*$$

\_e in lower energy (bonding orbital)

\_e in higher E (antibonding orbital)

Bond order =  $\frac{1}{2}(4-2) = 1$ 

For C<sub>2</sub>:  $(\sigma_{2s})^2(\sigma_{2s}^*)^2(\pi_{2px}^*)^2(\pi_{2py}^*)^2$ 

\_e in lower energy (bonding orbital)

Bond order =  $\frac{1}{2}(4-2) = 1$ 

Bond order =  $\frac{1}{2}(6-2) = 2$ 

$$\Delta E_d = \underline{\qquad}$$

$$\Delta E_d = \underline{\qquad}$$

Please note that complete MO diagrams for  $B_2$  and  $C_2$  must include the  $2p_Z$  molecular orbitals even if no electrons are in those orbitals.

# Bonding MOs formed by LCAO of 2p,

σ: cylindrically symmetric with no nodal plane about the bond axis

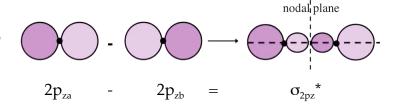
$$2p_{za} + 2p_{zb} = \underline{\hspace{1cm}}$$

Nodes pass through nuclei, but no nodes along the bond axis.

**Constructive** interference results in a region of **increased** amplitude between nuclei, and thus an **increased** probability density between nuclei (therefore **lower** energy MO)

# Antibonding MOs formed by LCAO of 2pz

σ: cylindrically symmetric with no nodal plane about the bond axis

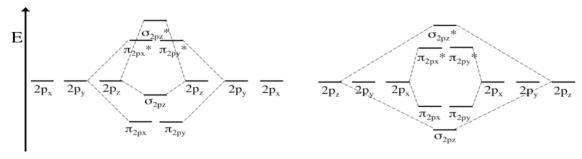


Nodes pass through and between the nuclei, but no nodes along the bond axis.

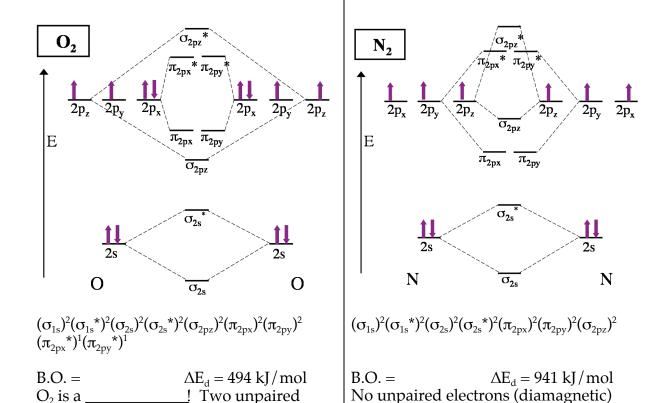
**Destructive** interference results in **a nodal plane between the nuclei**, and **decreased** probability density between nuclei (therefore **higher** energy MO)

The relative energies of the  $\sigma_{2pz}$  orbital compared to the  $\pi_{2px}$  and  $\pi_{2py}$  orbitals depend on the\_\_\_\_\_ value of the atoms.

For simple **homonuclear** diatomic molecules:



- The relative E ordering is  $(\pi_{2px})$  and  $(\pi_{2py}) < (\sigma_{2pz})$  if  $Z < \underline{\hspace{1cm}}$ .
- The relative E ordering is  $(\sigma_{2pz}) < (\pi_{2px})$  and  $(\pi_{2py})$  if  $Z = or > _____.$
- The relative E ordering of antibonding orbitals doesn't change with Z.



MO theory does a better job describing the properties of  $O_2$  than Lewis Structures do. Both MO theory and Lewis Structures do a good job with  $N_2$ .

<u>Note:</u> Molecules possessing **unpaired** electrons are <u>paramagnetic</u> (attracted by magnetic field); those in which the electrons are paired are <u>diamagnetic</u> (repelled by magnetic field).

#### C. For HETERONUCLEAR diatomic molecules:

- The relative E ordering is  $(\pi_{2px})$  and  $(\pi_{2py}) < (\sigma_{2pz})$  if Z < 8 for both atoms.
- You are NOT responsible for predicting the energy level ordering if either one of the atoms has Z = or > 8.

#### For full credit on MO diagrams,

electrons (paramagnetic)

- ➤ label increasing energy with an arrow next to the diagram.
- > pay attention to whether the question asks for *valence* electrons or *all* electrons.
- ➤ for any bonding orbital drawn, include the corresponding anti-bonding orbital, even if it is not filled with any electrons.
- ▶ label each atomic orbital (1s, 2s, 2px, 2py, etc.) and each molecular orbital ( $\int 2s$ ,  $\pi 2px$ ,  $\pi 2py$ , etc.) that you draw.
- ▶ fill in the electrons for both the atomic and molecular orbitals.

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